

# Sequential Estimation of Microbial Inactivation Arrhenius Parameters for Nonisothermal Heating Processes

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## Abstract

Most thermal food processes are nonisothermal. Better estimates of the kinetic parameters can be made using more realistic nonisothermal data. When the nonisothermal model is used, an inherent difficulty arises in estimation of the Arrhenius parameters (rate constant and activation energy) because of high correlation between them. The objective of this work was to show how to best estimate kinetic parameters for microbial inactivation.

Survival data of *B. Stearothermophilus* spores in canned pea puree, heated at retort temperatures of 104.4, 112.8, and 120.6°C for times 19-305 minutes were used. Temperatures in the pea puree were predicted over time using the solution to the analytical heat conduction equation. The kinetic parameters  $D_{108C}$  (89.7 min) and  $z$  (11.36 °C) were estimated sequentially using an inverse technique with the maximum a posteriori method. The correlation coefficient between the parameters was minimized by iterating over the reference temperature ( $T_r$ ). Scaled sensitivity coefficients for the two parameters were plotted to determine if any linear dependence existed. Both sequential estimation performance (coming to a constant) and linear independence of the sensitivity coefficients were highly sensitive to choice of the reference temperature. The impact of the results is that researchers using Arrhenius models should determine and use the optimum reference temperature to ensure that parameters can be estimated with low correlation and no convergence difficulties.

## Objectives

- To determine the appropriateness of the nonisothermal model by estimating parameters sequentially (updating parameters with addition of each datum).
- To minimize the correlation between the Arrhenius parameters and to minimize the error in their estimation.

## Estimation of Kinetic Parameters

$$N(t) / N_0 = 2 \int \int 10^{\frac{-1}{D_r} \int_0^t 10^{\frac{T(r,z,t)-T_r}{z}} dt} r dr dz$$

For each can  $Y(t) = \log(N(t) / N_0) = \log(\text{survival ratio})$

$N(t)$  = microbial count at time  $t$ ,  $N_0$  = initial count

- Estimate  $D_r$  and  $z$  sequentially using maximum a posteriori
- Minimize  $D_r$  and  $z$  correlation by iteration to estimate optimum  $T_r$
- Plot the scaled sensitivity coefficients

## Sensitivity Coefficients

Sensitivity coefficient ( $X$ ) is the first derivative of the function involving the parameter  $p_i$ , with respect to  $p_i$ .  $X'$  is the scaled  $X$  having the same units as  $Y$ . ( $\delta b = p_i^* \cdot 0.0001$ )

Finite difference method  $X'_{p_i} \equiv p_i \frac{y(p_i + \delta b) - y(p_i)}{\delta b}$

## Materials & Methods



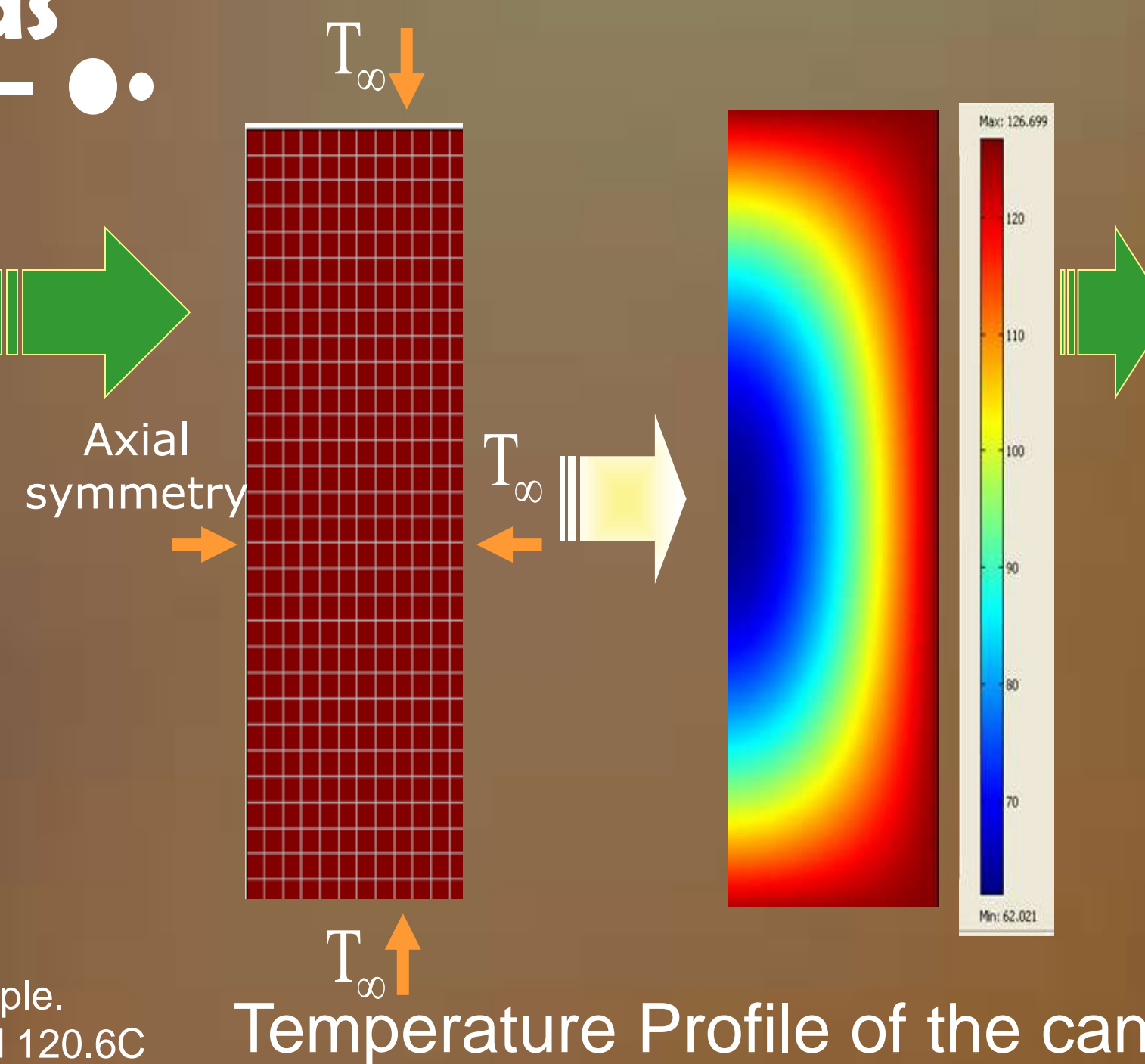
Pea puree sealed in can with thermocouple. Cans heated in steam at 104.4C, 112.8C, and 120.6C



Pea puree inoculated with  $9 \times 10^5$  cfu/ml *B. stearothermophilus* spores.  $k = 0.4$  W/mK,  $C_p = 3850$  J/kg K

Beck, J.V., Arnold, K.J. (1977). Parameter estimation in engineering and science Wiley, NY.

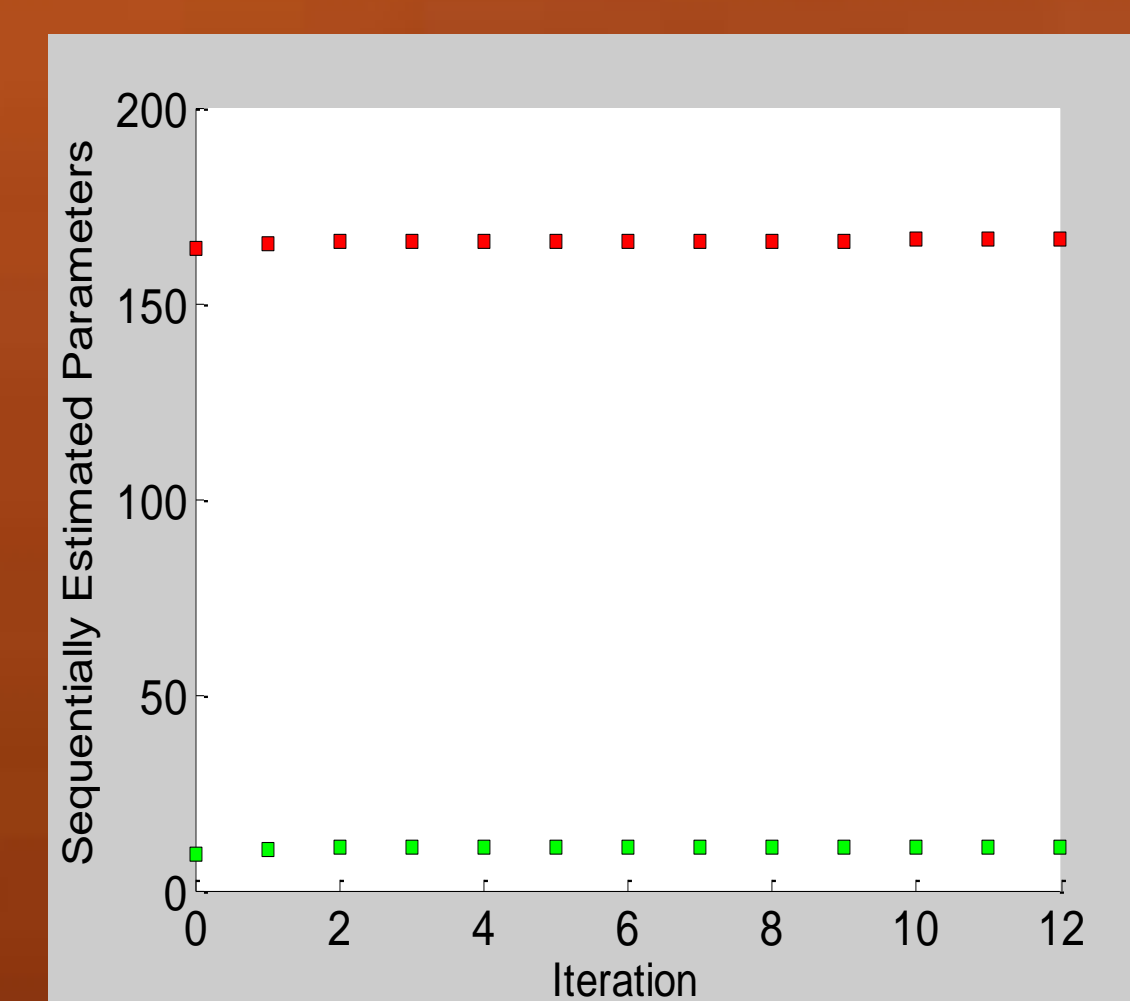
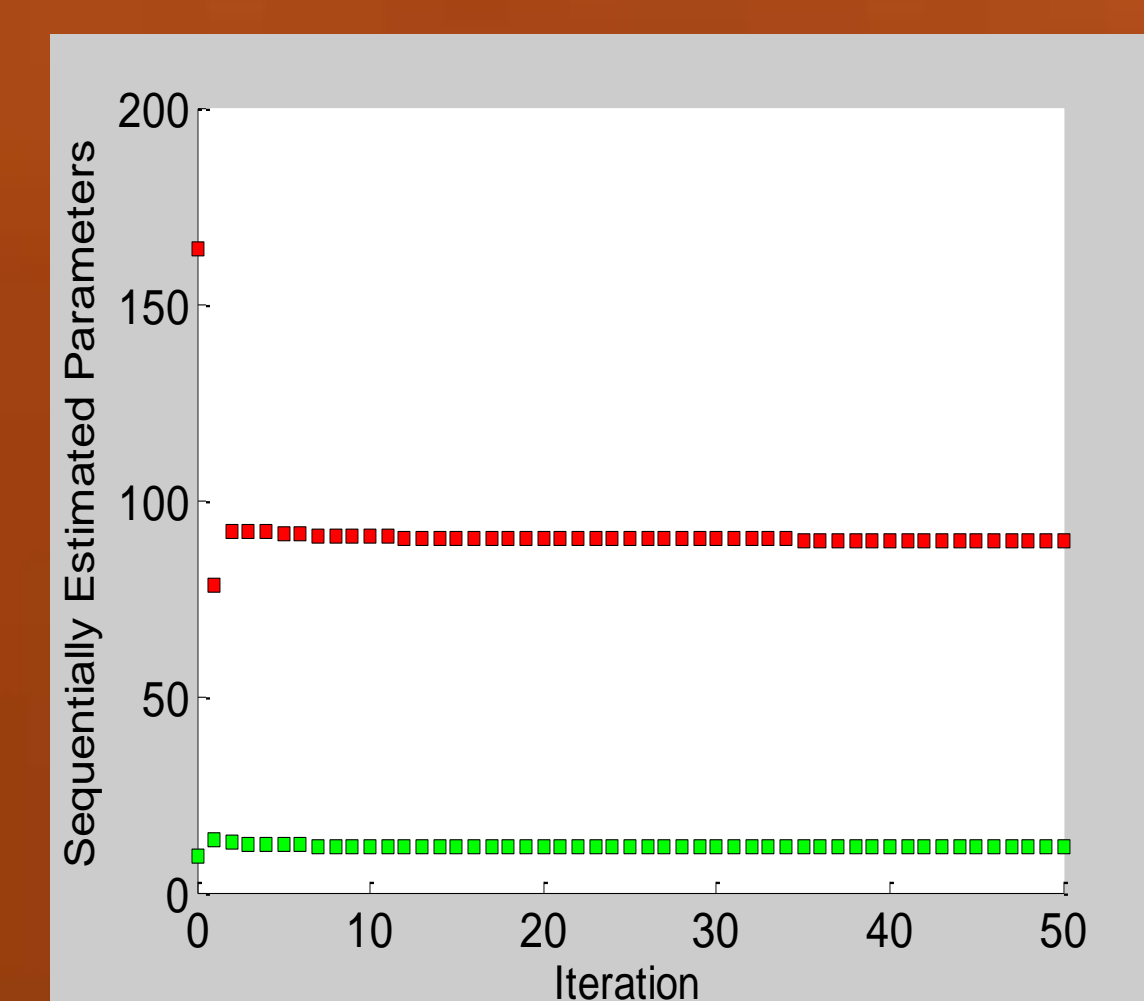
Welt, B. A. (1996). Kinetic parameter estimation in prepackaged foods subjected to dynamic thermal treatments, Ph.D. thesis, University of Florida, Gainesville, FL.



Temperature Profile of the can

Table 1. Retort temperature, heating time, and measured survival ratios for 24 heated cans (Welt, 1996).

Can number	Retort Temperature (°C)	Heating time (min)	Measured Survival ratios, $N/N_0$
1	n/a	0	0.891
2	n/a	0	1.109
3	104.4	50	0.689
4	104.4	50	0.769
5	104.4	90	0.656
6	104.4	90	0.744
7	104.4	180	0.387
8	104.4	180	0.476
9	104.4	180	0.279
10	104.4	180	0.266
11	104.4	240	0.0755
12	104.4	240	0.0697
13	104.4	240	0.0703
14	104.4	240	0.0667
15	104.4	275	0.0418
16	104.4	275	0.0401
17	104.4	305	0.00725
18	104.4	305	0.00855
19	112.8	27.5	0.642
20	112.8	32.5	0.433
21	112.8	44	0.159
22	120.6	19	0.500
23	120.6	24	0.266
24	120.6	27.5	0.093

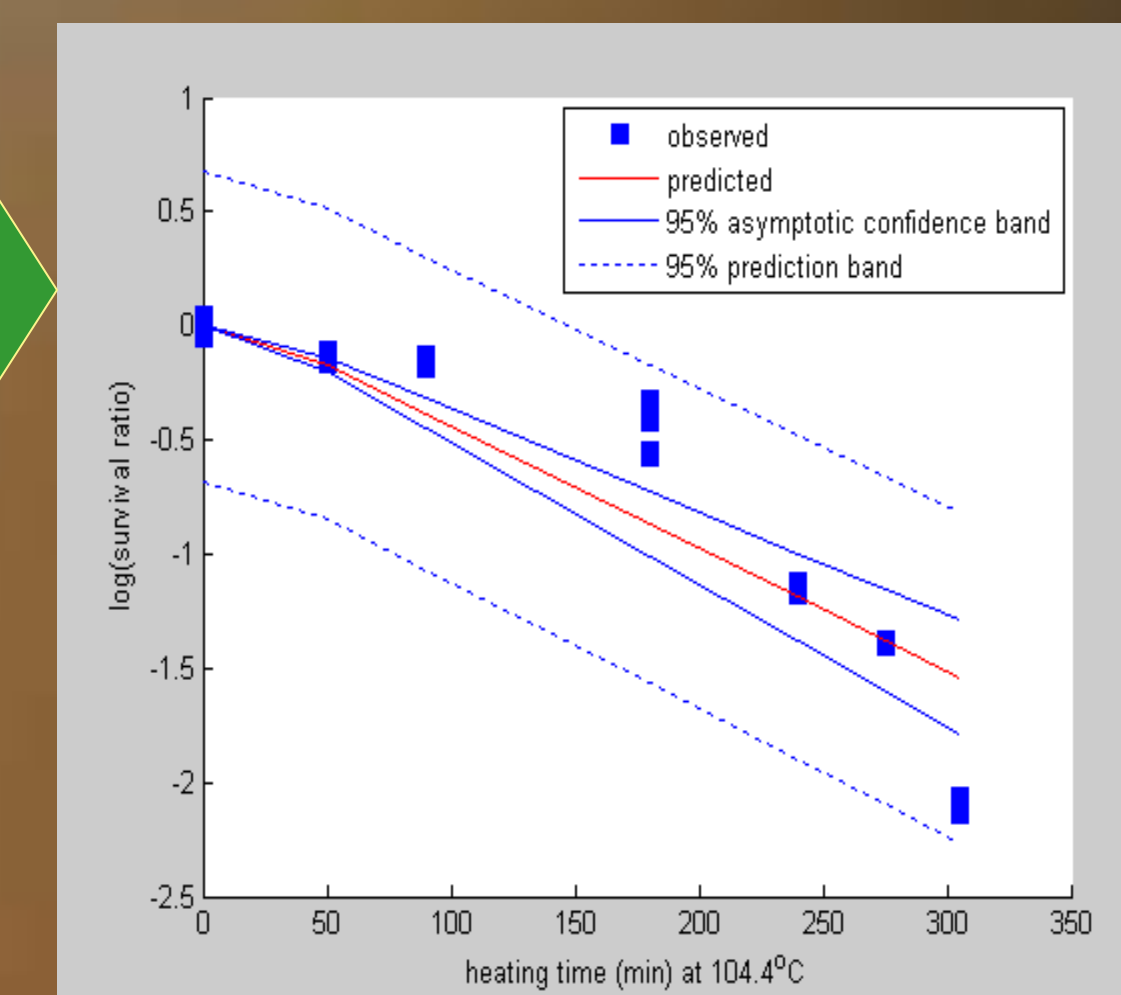


Sequentially estimated parameters  $D_r$  and  $z$  for  $T_r = 108C$  (left) and optimum  $T_r = 104.95C$  (right).

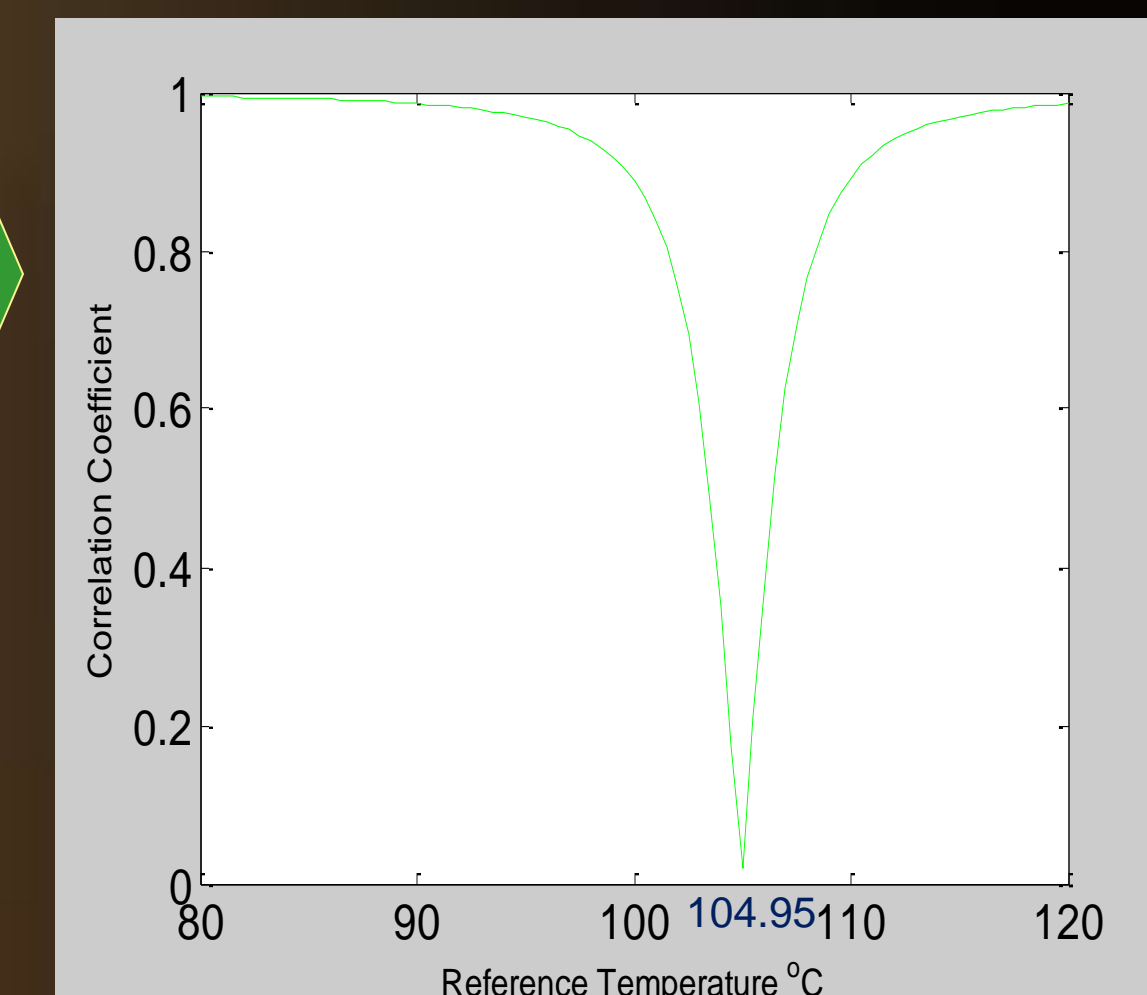
Confidence intervals (CI) of  $D$  and  $z$  vs.  $T_r$

$T_r$ (C)	$D_{121}$	$DCI_{lower}$	$DCI_{upper}$	$DCI_{width}$	$z$	$zCI_{width}$
120	6.28	1.63	10.94	9.31	11.35	5.43
108	6.28	5.07	7.49	2.42	11.35	5.43
104.95	6.28	5.50	7.06	1.56	11.35	5.43
95	6.28	3.15	9.42	6.27	11.35	5.43
75	6.28	-2.89	15.45	18.34	11.35	5.43

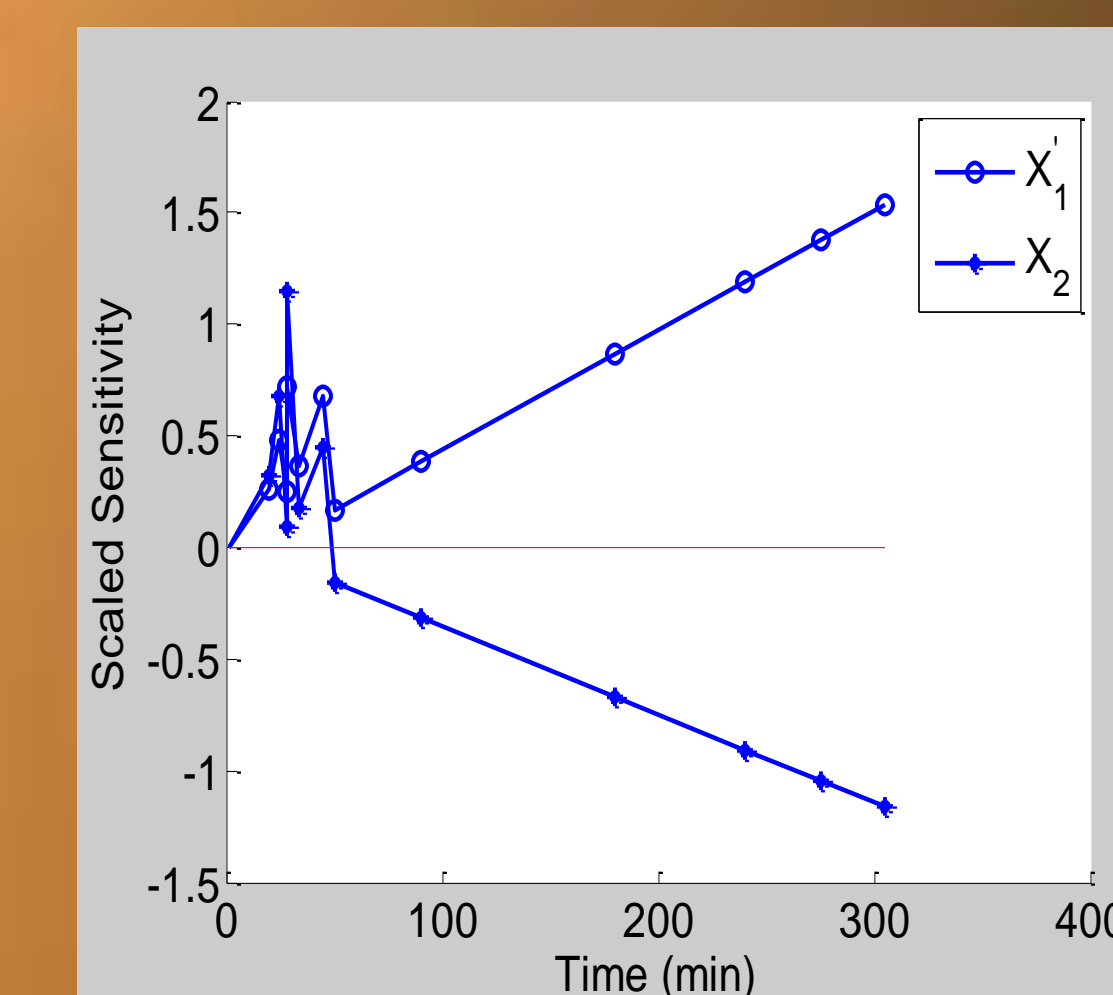
## Results



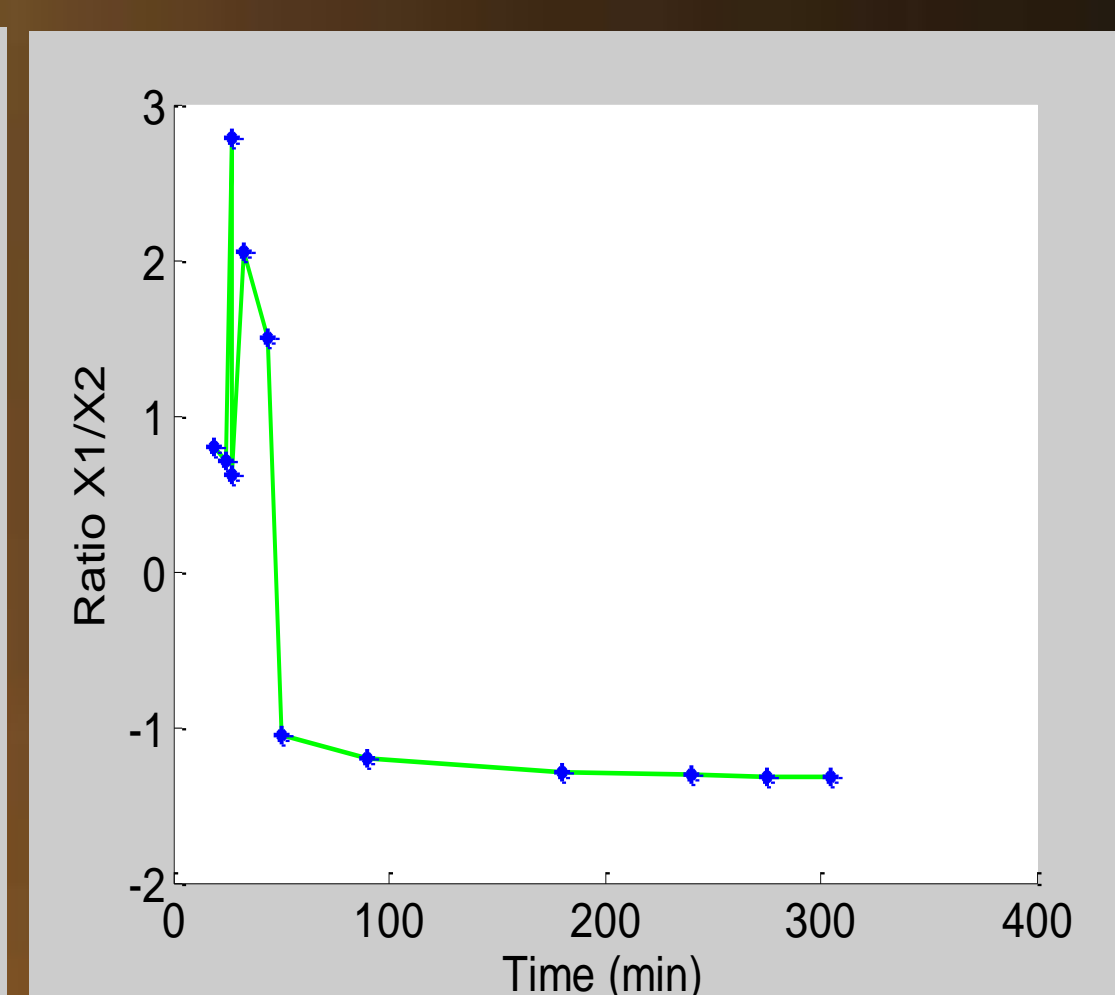
Predicted log survival based on estimated parameters  $D_{108C} = 89.7$  min,  $z = 11.4C$



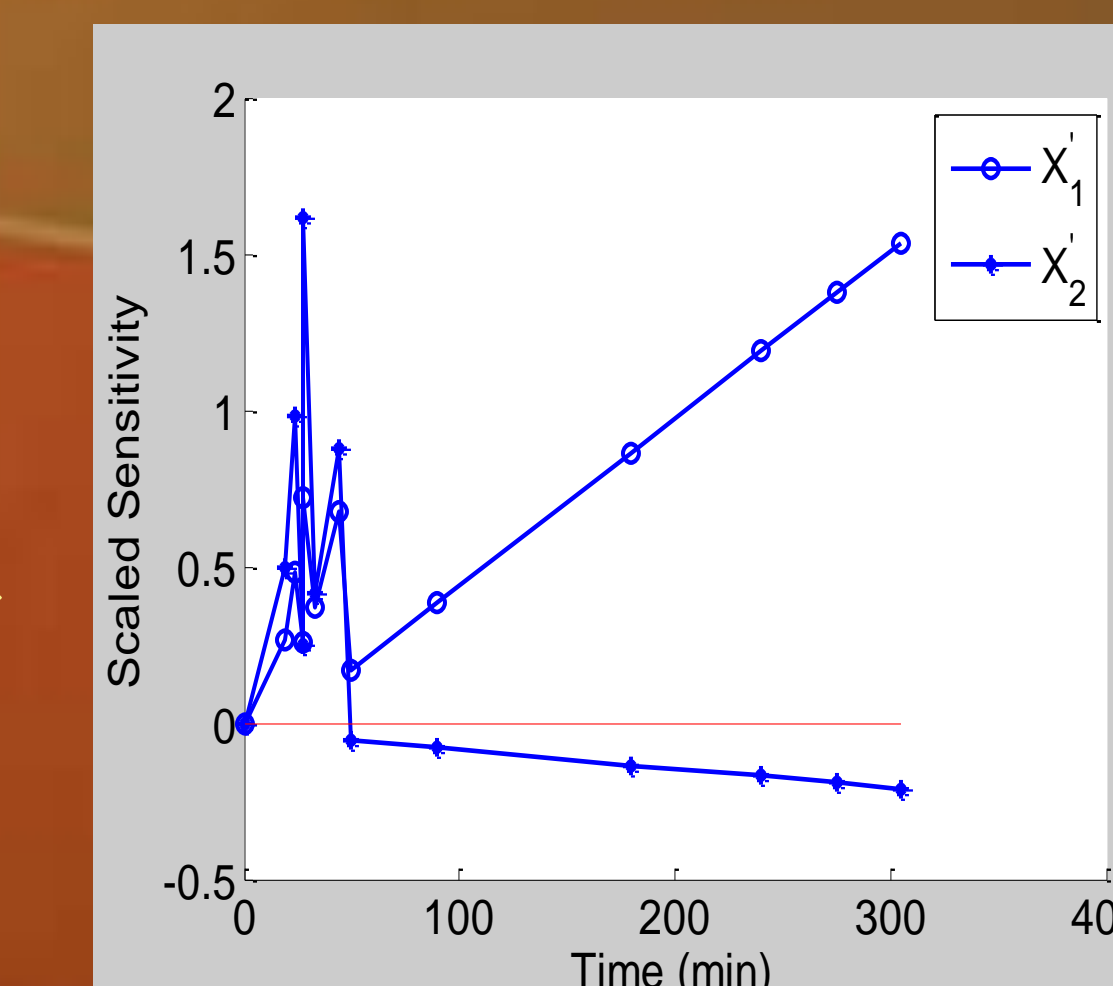
Correlation coefficient between  $D_r$  and  $z$  as a function of reference temperature  $T_r$



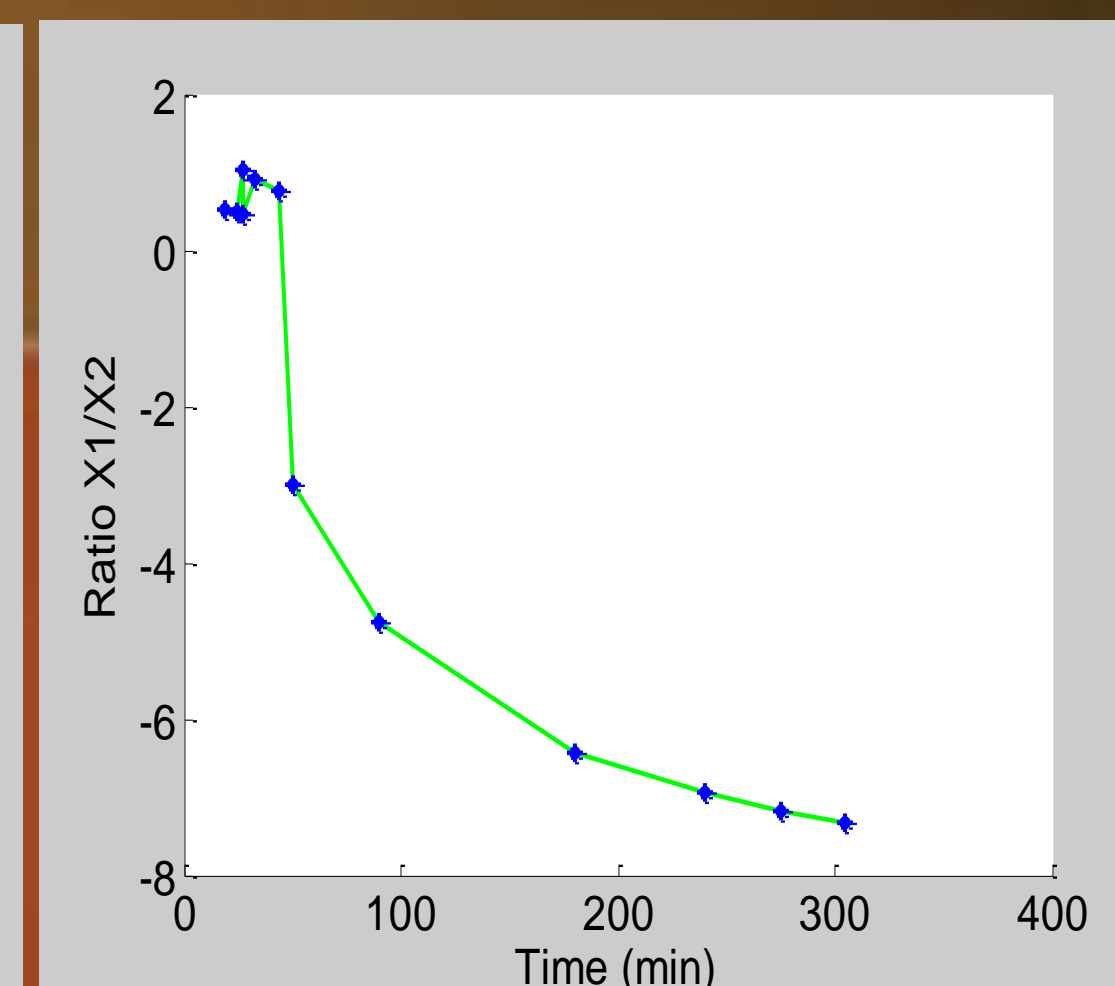
Scaled sensitivity coefficients of parameters  $T_r = 108C$



Ratio of sens coefficients at  $T_r = 108C$  shows linear correlation at heating time  $\geq 50$  min.



Scaled sensitivity coefficients for optimum  $T_r = 104.95C$



Ratio of sens coefficients at  $T_r = 104.95C$  shows linear independence for all times

## Conclusions

- Sequential estimation was faster for optimum Arrhenius  $T_r$  than for other  $T_r$
- Sensitivity coefficients were large and uncorrelated only at the optimum  $T_r$ ; at other  $T_r$ 's, they were linearly correlated for all heating times  $> 50$  min.
- Confidence interval and standard error for  $D_r$  was smallest at optimum  $T_r$ .
- Therefore, researchers using the Arrhenius model should minimize correlation coefficient between the parameters.